

## The 2016 Mathematics MCA-III Benchmark Report

The Mathematics MCA-III Benchmark Report is a tool that educators can use to compare the performance of students in their school on content benchmarks **relative to their overall performance** on the Mathematics MCA-III. That is, a school’s performance on each benchmark is described in terms of a deviation around the performance expected given its students’ scores on the entire test. The first section of this document presents an introduction to the benchmark reports and their interpretation. The second section presents a more-detailed discussion of the technical details involved in the calculations that are displayed in the reports.

The 2016 Mathematics MCA-III Benchmark Reports are organized by the content strands in the Minnesota Academic Standards for Mathematics (2007). A separate graph is produced for each strand to report school performance on the benchmarks that the strand comprises. The content strands assessed in each grade are displayed in Table 1. A list of the benchmarks assessed by the Mathematics MCA-III is included in the document *MCA-III Test Specifications: Mathematics, Grades 3–8 (2007 Standards)* available on the Test Specifications page of the MDE website. [View the Test Specifications page](#) (MDE > Educator Excellence > Districts, Schools and Educators > Statewide Testing > Test Specifications).

**Table 1**

**Mathematics MCA-III Strands**

Grades 3 to 5	Grades 6 to 8	Grade 11
1. Number & Operation 2. Algebra 3. Geometry & Measurement 4. Data Analysis	1. Number & Operation 2. Algebra 3. Geometry & Measurement 4. Data Analysis & Probability	2. Algebra 3. Geometry & Measurement 4. Data Analysis & Probability

### How to Read the Online Mathematics MCA-III Benchmark Reports

Figure 1 displays the performance for a school on five benchmarks from the grade 6 Algebra strand. Each plotted point represents performance on a benchmark (identified by its numeric label) relative to overall performance expectation for the school (represented by the dashed vertical line that crosses the x-axis at value 0.50). The relative performance on benchmarks for students within a school is reported using the Common Language Effect Size (CLES). When benchmark performance for a group of students is equivalent to that expected given their overall MCA scores, the CLES will equal 0.50. CLES values greater than 0.50 indicate that performance on the benchmark by students at the school exceeds that expected from their overall scores. CLES values less than 0.50 have the opposite implication: school performance on the benchmark is lower than expected based on the overall MCA scores of students in the school.

In addition to markers showing the school’s relative performance on each benchmark, a synthetic state-wide reference line (the solid gray vertical line) is included in the report to add a normative perspective. This state-wide reference line reflects the performance expected from students at the state mean for that grade in overall mathematics ability compared to that expected from students in the school across **all** items. Thus, the CLES value associated with state vs. school reference lines reflects global, rather than benchmark or strand-specific differences in performance expectations. When the CLES value for the state reference line is

greater than 0.50, it indicates that overall expected state performance is greater than expected school performance; values less than 0.50 have the opposite meaning.

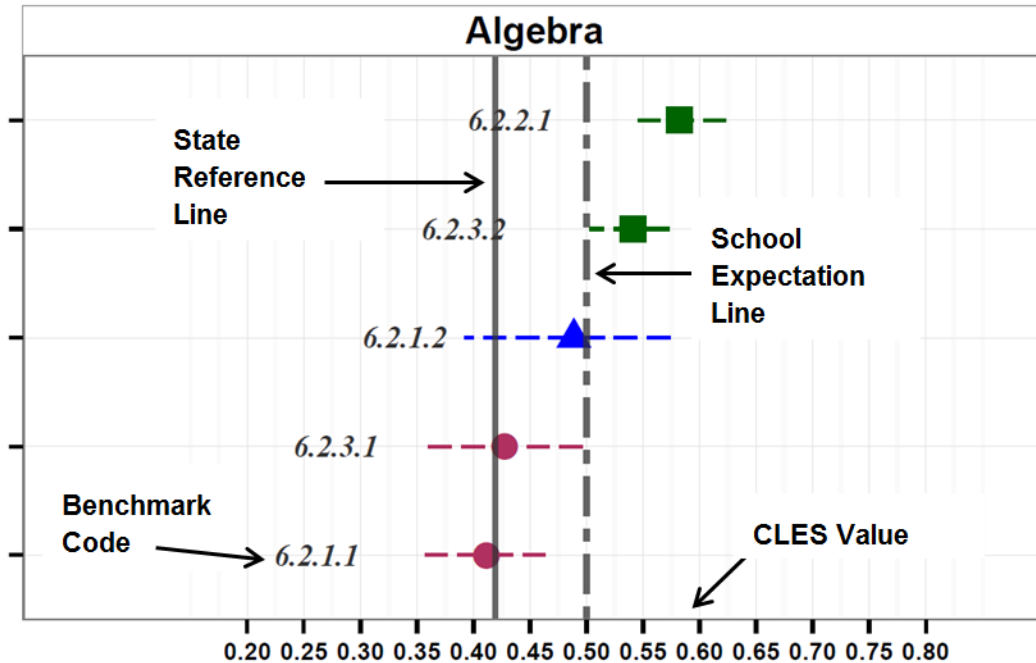





Figure 1. Sample Benchmark Report for the Algebra Strand in Grade 6.

### Benchmark Indicators

Individual benchmarks within each strand are identified by a 4-digit code. Relative performance on each benchmark is indicated by a color- and shape-coded symbol and a dashed line extending from the symbol. The symbol's horizontal position indicates the actual effect size value for the benchmark (on the CLES metric). The dashed line around the symbol represents a corresponding 95% credible interval (i.e., a 0.95 probability range of plausible CLES values given the data). Within each strand, the benchmarks are arranged from highest performance relative to the school at the top right of the graphic to lowest relative performance at the bottom left. As described in Table 2, the color and shape of each plotted symbol indicate how the school's students performed on the benchmark **relative to expectations** based on their overall Mathematics MCA-III scores. Because the state reference line is based on comparison of state vs. school expectations across *all* items, comparison of individual benchmark performance with the state reference line is not appropriate.

Table 2

### Benchmark Marker Color and Shape Codes

	<b>Green Square:</b> Students performed <u>significantly above</u> expectation on the benchmark. Assigned to markers to the <i>right</i> of the dashed vertical line with credible bands that do not overlap the line.
	<b>Blue Triangle:</b> Students performed <u>near</u> expectation on the benchmark. Assigned to markers with credible bands that overlap the dashed vertical line.
	<b>Red Circle:</b> Students performed <u>significantly below</u> expectation on the benchmark. Assigned to markers to the <i>left</i> of the dashed vertical line with credible bands that do not overlap the line.

## **Evaluating Performance Differences between Benchmarks**

In making comparisons between pairs of benchmarks, pay close attention to the amount of overlap of the credible bands for those benchmarks. If their credible bands overlap by more than one-half, regardless of color or position of the markers, performance on those benchmarks may be considered statistically equivalent. In other words, if the bands on two different benchmarks have substantial overlap, there is little credible evidence to suggest that actual performance was significantly different on the two benchmarks. If the credible bands across two benchmarks do not overlap, then there is very clear evidence of a reliable difference in performance between the two benchmarks.

## **Benchmark Codes**

Benchmark codes are indicated to the left of each marker. A list of the benchmarks assessed by the Mathematics MCA-III is included in the document *MCA-III Test Specifications: Mathematics, Grades 3–8 (2007 Standards)* available on the Test Specifications page of the MDE website. [View the Test Specifications page](#) (MDE > Districts, Schools and Educators > Statewide Testing > Test Specifications).

## **Cautions in Interpreting the Benchmark Report**

As with any data, caution must be exercised in making inferences from the benchmark report. It is important to frame any interpretation within the context of the school's environment. Consideration of external information about the Mathematics curriculum, instructional practices and data from other classroom assessments is critical to making appropriate and meaningful inferences from this report. Interpretation of this report should also take the following factors into account:

- The generalizability of inferences about student performance in the content domain that the benchmark comprises depends upon the representative sampling of: (a) items from the benchmark that students in a school are administered; and (b) students in a school who are administered items from the benchmark. For a computer-adaptive test, such as the online Mathematics MCA-III, there generally will be multiple items administered across students at a school assessing each benchmark.
- Adaptive test blueprint specifications are at the strand and standard level. Thus, benchmark coverage can vary for each student and school. In an adaptive test, this variation in coverage will depend to some degree on ability levels of the students in each school because benchmarks can vary in their inherent difficulty. The length of the credible band around a benchmark report marker reflects, in part, the number of item responses included in calculating the benchmark CLES value; shorter credible bands are associated with larger numbers of student responses to items from the benchmark.
- Different sets of students may be administered items from any particular benchmark. Some benchmarks may have an item by student ability interaction which would result in lower ability students being either over- or under-represented on responses to items from a benchmark.

There are several misinterpretations that should be avoided:

- Color/shape and position of markers in the graphs **do not** reflect benchmark difficulty.
- Color/shape and position of markers in the graphs **do not** correspond to achievement levels (i.e., Does Not Meet, Partially Meets, Meets, or Exceeds the Standards).
- When comparing Benchmark Report graphs from different schools within a district, be aware that the range of values on the horizontal axis CLES scale is adjusted to fit each school's data. If a school has a large outlier (i.e., a benchmark with very high or very low relative performance) the graph will have a greater range reflected on the horizontal axis, and its

benchmark markers will appear to be clustered more tightly together than those for a school with a smaller range of benchmark CLES values.

The primary purpose of the MDE Benchmark Report is to provide information to help curriculum and instructional staff in making inferences about their instructional/curricular activities and their students' level of understanding, based on performance data from the online Mathematics MCA-III. The purpose of data in this report is **not** to designate strengths and weaknesses in the school. Rather, the Benchmark Report is to serve as a guidance tool to identify possible gaps in instructional content that the school staff may find relevant and important. In particular, it is important to recognize that this report reflects data on a sample of student testing behavior obtained at a single time point in the academic year, and may not fully reflect the systematic instructional and curricular outcomes as a whole. Furthermore, some of the results may depend upon the timing and sequence of when content was presented during the school year. For those reasons, it is critical to appropriately involve knowledgeable instructional staff in the discussion and interpretation of the results, and in deliberations about their implications for curriculum and instructional activities.

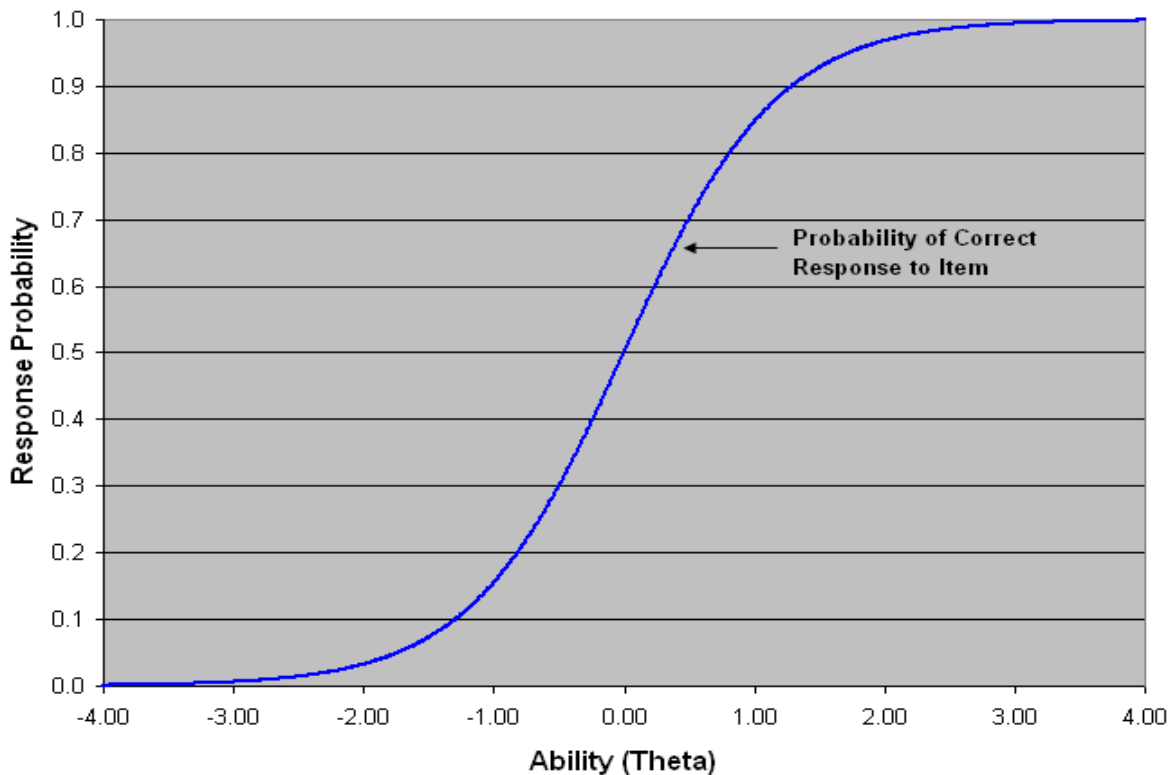
## Technical Details for the Mathematics MCA-III Benchmark Reports

### ***Relative Benchmark Performance and Common Language Effect Size***

The relative performance on benchmarks for students within a school or district is reported using the Common Language Effect Size (CLES). The CLES is a non-parametric statistic used to summarize group differences. The basic notion is that two groups (say, Group A and Group B) exist, where each group member has a score on an outcome of interest. The CLES is calculated as the probability that a randomly selected member from one group (e.g., Group A) will have a higher score than a randomly selected member of the other group (Group B). When the groups are equivalent, the probability will be 0.50. As scores in Group A become increasingly higher than those in Group B, the probability that the score of a randomly selected member from Group A will be greater than that of a randomly selected member from Group B increases correspondingly, and the CLES becomes increasingly greater than 0.50. Conversely, as scores in Group A become progressively lower than those in Group B, the CLES will move progressively lower than 0.50.

The Mathematics MCA-III Benchmark report uses the CLES to compare performance of two groups on the items administered from a benchmark. The scores comprising the first group are the observed item scores for students in the school on items from the benchmark. The scores comprising the second group are the item scores on benchmark items that would be expected from each student, given their overall score on the Mathematics MCA-III. These expected scores (or *average conditional performance*) are calculated based on the 3-parameter logistic (3PL) measurement model that underlies all scaling on the MCA-III. The 3PL model estimates the probability of a correct response on each benchmark item given each student's overall MCA-III score (see Figure 2). Using MCA-III item response data from students in the school, the observed and expected numbers of correct and incorrect responses to items from each benchmark are obtained and used to calculate the CLES.

The School-Based CLES expresses the probability that an item score (0 or 1), selected at random from the observed set of scores on items representing a benchmark is greater than an item score (0 or 1) drawn at random from the expected set of benchmark item scores based on the 3PL model (i.e., average conditional performance). When the number of correct observed benchmark item responses is equivalent to the number of correct responses expected based on overall MCA-III scores, the result will be a CLES of 0.50.



**Figure 2. Sample item response function: Probability of correct response conditional on ability.**

**School or District Reference Line**

The gray dashed school expectation reference line located at 0.50 on the CLES scale on each benchmark report graph represents observed benchmark item performance equal to expected benchmark item performance. A benchmark CLES value greater than 0.50 indicates that student performance on items from the benchmark exceeds the expected conditional student performance. CLES values less than 0.50 have the opposite implication: school performance is lower than expectation given the ability of students who were administered the set of items from the benchmark. When CLES is calculated based on dichotomous item scores, the deviation from CLES value 0.50 is approximately equal to one-half the difference in proportions correct in the two groups. Thus, a benchmark CLES value of .55 can be interpreted to mean that the observed proportion of correct responses to benchmark items is 0.10 greater than the expected proportion correct.

**State Reference Line**

Although the focus of the Mathematics Benchmark Report is within-school comparisons of observed and expected benchmark item score distributions, some users may be interested in comparing school and statewide performance on the CLES scale. In an adaptive testing context, comparison of observed state and school item scores is problematic because students are being administered items tailored to their ability level, and the difficulty of items taken by students in a school may be very different than what is typical statewide. The heuristic approach adopted in the benchmark report is to calculate the expected count of correct responses if a student whose mathematics ability was at the state average for the grade was administered the same items actually taken by students in the school. As before, a CLES index is calculated, this time comparing the expected correct response count (across all items) for the average state student vs. the students in the school. The gray solid vertical line plotted at the obtained CLES value represents state-wide performance **relative to the school or district**. When the solid state reference line

is to the right of the dashed school/district line (i.e.,  $>0.50$ ), it means the expected overall state performance exceeded that of the school. Conversely, when the state reference line is less than 0.50, it indicates expected state overall performance that is lower than expected performance for the school.

### **95% Credible Interval Bands**

The credible interval is the Bayesian analogue of the confidence interval reported in common statistical (i.e., frequentist) practice. The 95% credible interval band reported here can be interpreted as the range of CLES values within which there is a 95% probability the true CLES value lies, given the observed data. The 95% credible interval bands are estimated empirically, based on observed CLES values resulting from 20,000 paired random draws from beta binomial distributions with parameters (1+observed number correct, 1+observed number wrong) for the school observed data and (1+expected number correct, 1+expected number wrong) for the school expectation data. The .025 and .975 quantiles of the observed CLES sampling distribution serve as the limits of the 95% credible interval band. One consequence of this empirical approach is that when a district has a single school at a grade, the re-sampled distributions from school and district analyses can differ very slightly, and the resulting school and district benchmark graphs will be not quite identical.